

1. (15) Consider the Differential Equation $y'' - 2y' + 2y = 0$. Let $y_1(x) = e^x \sin x$; $y_2(x) = e^x \cos x$

a. Verify, using the definition, that $y_1(x)$ is a solution of the equation.

b. Find the Wronskian $W(y_1, y_2)$.

c. Explain why the solution in part b. shows that y_1, y_2 are linearly independent

2. Consider the IVP $y'' + y' - 2y = 2x$; $y(0) = 0$; $y'(0) = 1$.

a. (7) Find the complementary solution y_c of the associated homogeneous equation.

b. (7) Find a particular solution $y_p(x)$ by observing the form of $f(x)$ and making an educated guess, then substituting into the original DE and solving.

c. (8) Use y_c, y_p to find solution satisfying the IC

3. (12) Find a general solution to each differential equation

a. $y^{(3)} - 7y'' + 19y' - 13y = 0$

b. $y^{(4)} + y^{(3)} - 8y'' - 12y' = 0$

4. (16) Consider the 1st-order IVP $y' = y - x - 1$; $y(0) = 1$, with solution $y_a(x) = 2 + x - e^x$. Use Euler's method to approximate $y(1)$, with step size $h = .25$. Use the last column of the table to store the absolute difference between Euler's approximation to $y(x)$, and the value of $y_a(x)$, using 3 decimal places

i	x_i	Approx y_i	$y_a(x_i)$	Abs err
0	0.00	1.000	1.000	0.000
1				
2				
3				
4				

5. (14) Solve the IVP $y'' - 3y' + 2y = 3e^{-x} - 10\cos(3x)$; $y(0) = 1$, $y'(0) = 2$

MAT282 Exam 2

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2/26/2010

Siena Heights University

Problem	Possible Pts	Points
1	15	
2	22	
3	12	
4	16	
5	14	
6	20	
Total	99	

Your word problems for exam II are in this packet. The rules for take-home exam are:

1. You may use your book and any notes you have
2. You may ask me for hints
3. You may use your calculator
4. You may **not** discuss the work with your classmates or any other humans

The work is due at class time on March 8. I plan to be in the office on Friday the 5th for questions, or you can e-mail me during the week.

I certify that this exam is the result of my work and mine alone, I have received no help from any sources except those permitted as described in these instructions.

Signed,

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6. (20) Solve each applied problem

- a. Suppose that a local water supply is being contaminated slowly. The amount of contaminant is measured in parts per million, the population of which is denoted $A(t)$ and modeled by the equation $\frac{dA}{dt} = kA(t)(200 - A(t))$ where k is a constant. Suppose there are currently 100 ppm of the contaminant in the water, and it is growing at the rate of 1 ppm/yr.

i. Find a formula for $A(t)$

ii. How much of the contaminant will be in the water in 20 years?

iii. After how many years will the contaminant reach the unsafe level of 180 ppm?

